



$$\frac{\partial E(n)}{\partial w_{ji}} = \sum_{k=1}^P \sum_{r=1}^R \underbrace{\frac{\partial E(n)}{\partial e_r}}_{-1} \cdot \underbrace{\frac{\partial e_r}{\partial v_r}}_{-1} \cdot \underbrace{\frac{\partial v_r}{\partial w_{jk}}}_{f'(v_k)} \cdot \underbrace{\frac{\partial v_r}{\partial z_k}}_{f'(v_k)} \cdot \underbrace{\frac{\partial z_k}{\partial w_{ji}}}_{w_{kj}} \cdot \underbrace{\frac{\partial z_k}{\partial v_j}}_{f'(v_j)} \cdot \underbrace{\frac{\partial v_j}{\partial w_{ji}}}_{x_i}$$

$$= -f'(v_j) \left[\sum_{r=1}^P f'(v_k) \left(\sum_{r=1}^R f'(v_r) e_{rk} \right) \cdot w_{kj} \right] x_i = -f'(v_j) \cdot \left[\sum_{k=1}^P \delta_{rk} w_{rk} \right] w_{kj} x_i = -f'(v_j) \left(\sum_{k=1}^P \delta_{rk} w_{rk} \right) x_i$$